

Noninvasive Electrical Characterization of Materials at Microwave Frequencies Using an Open-Ended Coaxial Line: Test of an Improved Calibration Technique

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Abstract—We consider dielectric measurements using a probe consisting of coaxial transmission line with an open-circuit end placed against the sample. For the 2.99 or 3.6 mm (OD) probes considered in this study, a simple lumped parameter model shows errors above 1 GHz that increase greatly with frequency. We evaluate an approximate model due originally to Marcuvitz, on the basis of measured probe impedances from 1 to 18 GHz with samples consisting of water, methanol, and dioxane–water mixtures. This model is more accurate than the lumped-parameter model, and is better suited for calibration of the automated network analyzer. Finally, we consider the errors introduced in dielectric measurements by the use of approximate models for the probe. The technique succeeds because of partial cancellation of errors in modeling the probe in ANA-based measurements.

I. INTRODUCTION

SEVERAL AUTHORS have described the use of open-ended coaxial transmission lines as sensors for measurement of the complex permittivity ϵ of materials at microwave frequencies [1]–[6]. The probe (typically a length of the common 3.6 mm OD semirigid line) is placed against the sample and its complex reflection coefficient Γ is measured with an automated network analyzer (ANA). The ANA is calibrated by measuring the reflection coefficient of the line with known loads, typically open and short circuits and a reference liquid such as water. A good electrical model for the probe is needed, both to calibrate the ANA and to calculate the dielectric properties of the sample from the probe admittance.

In the limit of low frequencies, the admittance Y of the probe is given by a lumped-parameter model:

$$Y = C_0 + j\omega C_f(\epsilon' - j\epsilon'') \quad (1)$$

Manuscript received February 10, 1989; revised August 21, 1989. This work was supported by the National Science Foundation under Grant ECS-8717857 (D. Misra and M. Chabba), by the National Institutes of Health under Grant CA26046, and by the Office of Naval Research under Contract N00014-86-K-0240 (K. R. Foster and M. Mirotznik).

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IEEE Log Number 8931564.

where C_0 and C_f are constants that depend on the dimensions of the probe, ω is the frequency (rad/s), and $\epsilon = \epsilon' - j\epsilon''$ is the complex permittivity of the sample.

As the frequency is increased, this model fails because of the presence of higher order modes at the aperture and (at still higher frequencies) because of radiation effects. While no rigorous closed-form solution exists, several approximate solutions are available. Marcuvitz expressed the admittance of a probe as an integral over its aperture [7]; this approximation was rederived in equivalent forms by Levine and Papas [8] and Misra [9]. Marcuvitz's approximation can be expanded in a series that is convenient for numerical solution, and in this form has been used in experimental studies employing the probe technique [10]. Alternatively, the probe admittance can be numerically calculated using the mode-matching technique [11]. This method explicitly takes higher order modes into account and is more accurate but too time-consuming for microcomputer-based measurements.

As shown below, Marcuvitz's approximation is only a modest improvement over the lumped-parameter model for the probes considered here. However, for ANA-based measurements it significantly enhances measurement accuracy. The reason, apparently, is a cancellation of errors; errors in calibrating the ANA are partially compensated by subsequent miscalculation of the permittivity from the (mismeasured) admittance. (The ANA is still miscalibrated, however, which might lead to imperfect cancellation of resonance-type artifacts [12].)

II. THEORY

The two equivalent formulations for the admittance of the line are

$$Y = j \frac{k^2 Y_0}{\pi k_c \ln(b/a)} \int_a^b \int_a^b \int_0^\pi \cos \phi' \frac{\exp(-jkr)}{r} d\phi' d\rho' d\rho \quad (2)$$

where $r = \{\rho^2 + \rho'^2 - 2\rho\rho' \cos \phi'\}^{1/2}$ and $Y_0 = 0.02S$, the

TABLE I
PARAMETERS FOR THE COAXIAL TRANSMISSION LINES
USED FOR THIS STUDY

o.d.	.36	.299
a (cm)	.0456	.040
b (cm)	.1490	.1140
ϵ_c	2.1	1.58
I_0	.1798	.1225
I_1	6.17 (-4)	2.54 (-4)
I_2	-2.95 (-6)	-7.34 (-7)
I_3	4.74 (-9)	7.05 (-10)
I_4	-4.37 (-12)	-3.86 (-13)
I_5	2.71 (-15)	1.41 (-16)
I_6	-1.22 (-18)	-3.74 (-20)

The outer diameter (o.d.) is nominal only and used for reference in the discussion in the text.

Exponents are indicated in parentheses.

characteristic admittance of the line (from Misra). In addition,

$$Y = G + jB$$

$$G = \frac{Y_0 \sqrt{\epsilon}}{\ln(b/a) \sqrt{\epsilon_c}} \int_0^{(\pi/2)} \frac{1}{\sin \theta} [J_0(k_0 \sqrt{\epsilon} b \sin \theta) - J_0(k_0 \sqrt{\epsilon} a \sin \theta)]^2 d\theta$$

$$B = \frac{Y_0 \sqrt{\epsilon}}{\pi \ln(b/a) \sqrt{\epsilon_c}} \int_0^{\pi} [2 \text{Si}(k_0 \sqrt{\epsilon} (a^2 + b^2 - 2ab \cos \theta)) - \text{Si}(2k_0 \sqrt{\epsilon} a \sin(\theta/2)) - \text{Si}(2k_0 \sqrt{\epsilon} b \sin(\theta/2))] d\theta \quad (3)$$

(from Marcuvitz). In these expressions, a and b are the inner and outer radii of the line (Table I); k_0 is the propagation constant in free space, $2\pi f/c$, where c is the velocity of light in vacuum and f the frequency; ϵ and ϵ_c are the relative permittivities of the material under test and the dielectric in the transmission line, respectively; J_0 is the Bessel function of order zero; and Si is the sine integral.

These results are approximate in several respects: they were derived assuming the presence of an infinite conductive flange over the aperture (not present with the coaxial lines), and they do not explicitly account for higher order modes at the aperture. In addition, the properties of any real probe will vary because of manufacturing tolerances.

In this study we evaluated (2) and (3) numerically, using either a series expansion or numerical integration. The Appendix contains a series expansion that is valid for the frequency range and probe dimensions used in this study. (Fewer terms in this expansion are reported in [10].) In the lumped-parameter model, the parameter C_f corresponds to

TABLE II
DISPERSION PARAMETERS USED WITH EQ. (4) TO CALCULATE
THE DIELECTRIC PROPERTIES OF THE FLUIDS USED IN THIS STUDY

Substance	ϵ_{∞}	ϵ_s	$\tau \times 10^{11}$ (Sec)	α
water	5.2	78.5	8.3	0
80% water- 20% dioxane	3.75	61.9	1.1	0
60% water- 40% dioxane	3.35	44.5	1.5	0.1
40% water- 60% dioxane	3.1	27.2	1.7	0.1
20% water- 80% dioxane	3.75	11.9	2.3	0.1
dioxane	2.2	2.2	—	—
methanol	5.6	32.6	4.8	0

Values for water and methanol from [14].

For the dioxane-water mixtures, ϵ_s was obtained from [15] and the dispersion parameters for these solutions estimated by interpolation from [16].

Temperature is 25°C.

the term $B1$ in the Appendix, divided by the frequency; C_0 is small and is neglected for present purposes.

III. EXPERIMENTAL

For the experiments, probes were constructed from lengths of semirigid 50 Ω coaxial line (3.6 mm OD line with a type SMA connector, or 2.99 mm OD precision line with a precision type K connector) ranging in length from 9.5 to 14 cm. The end distal to the connector was machined flat and polished with fine crocus cloth. The 2.99 mm line and K connector have considerably higher precision than 3.6 mm line and SMA connector, and were used for most of the measurements discussed below.

The reflection coefficients of the probes were measured from 0.1 to 18 GHz using a Hewlett-Packard model 8510 ANA. For these measurements, the ANA was calibrated using the normal factory-standard calibration loads (short circuit, open circuit, 50 Ω sliding and fixed loads) at the end of a length of precision flexible test cable. A probe was then connected to the test cable, taking care not to flex the cable. The reference plane of the measurement was defined by shorting the end of the probe with aluminum foil and adjusting the electrical delay of the ANA until a constant 180° phase angle was observed. The small reflection from the connector on the coaxial line was removed using the time-domain gating feature of the ANA. In this procedure, the measured reflection coefficients were transformed into the time domain, the connector reflection was electronically gated out, and the data were then transformed back into the frequency domain.

Measurements were conducted from 0.1 to 18 GHz on several reference liquids: water, methanol, and various water-dioxane mixtures. The dielectric properties of these

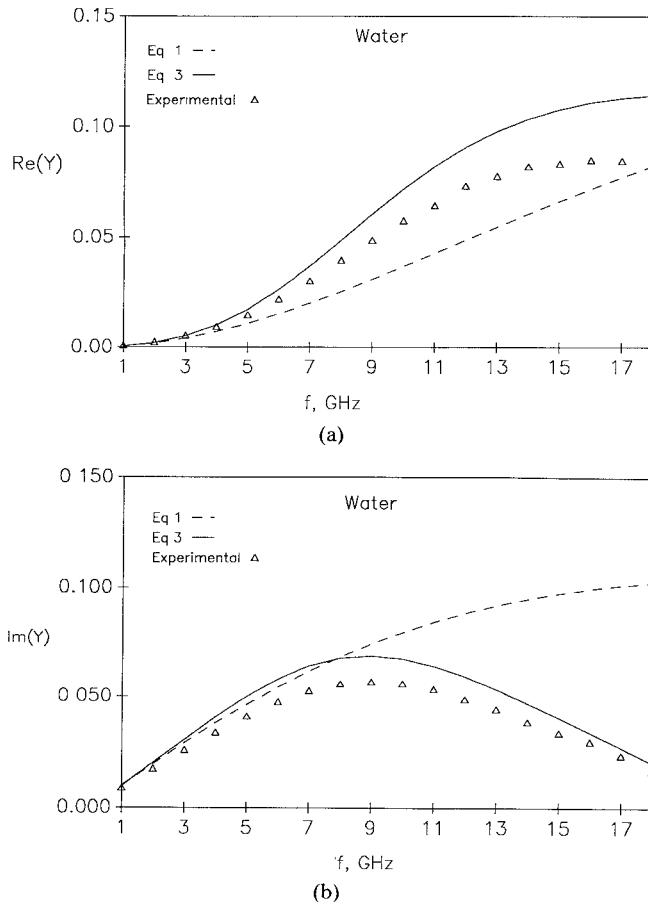


Fig. 1. Measured and calculated admittances of 2.99 mm (OD) open-ended coaxial transmission line immersed in water. (a) Real part. (b) Imaginary part.

liquids are summarized by the empirical equation

$$\epsilon = \epsilon_{\infty} + \frac{\epsilon_s - \epsilon_{\infty}}{1 + (j\omega\tau)^{1-\alpha}} \quad (4)$$

with parameter values summarized in Table II. Measurements were conducted at 20–25 °C.

Figs. 1 and 2 compare the measured admittance of the 2.99 mm probe when immersed in methanol and water with Marcuvitz's approximation (eq. (3)) and the lumped-parameter model (eq. (1)). Marcuvitz's approximation works quite well for methanol over the entire frequency range of the measurements; it is less satisfactory for water. The errors in the reflection coefficient (given as the magnitude of the difference between the measured and calculated reflection coefficients) for water at 10 GHz are 0.06 (Marcuvitz's approximation) and 0.14 (lumped-parameter model). For methanol at 10 GHz these errors are 0.02 and 0.04 respectively. Marcuvitz's approximation is clearly an improvement over the lumped-parameter model, although the errors involved considerably exceed those of factory-standard calibration loads for ANA calibration. (Another source of error, not considered here, is the uncertainty in the dielectric properties of the reference liquids, which can be several percent at microwave frequencies.)

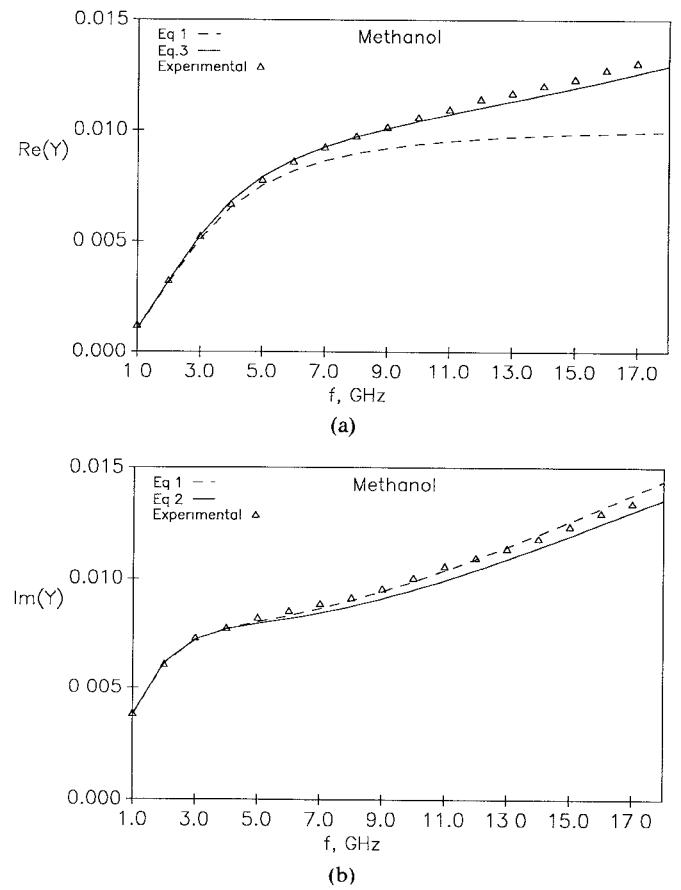


Fig. 2. Measured and calculated admittances of 2.99 mm (OD) open-ended coaxial transmission line immersed in methanol. (a) Real part. (b) Imaginary part.

IV. CORRECTIONS TO THE MEASURED ADMITTANCE

We compare the lumped-parameter model and Marcuvitz's approximation for ANA calibration. The formalism for such corrections is well known. If Γ_M is the measured reflection from a load (the coaxial aperture terminated by the sample) whose true reflection coefficient is Γ_L ,

$$\Gamma_L = \frac{\Gamma_M - S_{11}}{\Gamma_M S_{22} - \Delta} \quad (5)$$

where $\Delta = S_{11}S_{22} - S_{21}S_{12}$ and $\{S_{ij}\}$ are the elements of the scattering matrix representing the two-port network. The elements of S can be found from measurements on three standard loads.

Equation (5) can be used to derive an alternate formulation:

$$\frac{(Y_L - Y_1)}{(Y_L - Y_2)} \frac{(Y_2 - Y_3)}{(Y_3 - Y_1)} = \frac{(\Gamma_M - \Gamma_1)}{(\Gamma_M - \Gamma_2)} \frac{(\Gamma_2 - \Gamma_3)}{(\Gamma_3 - \Gamma_1)} \quad (6)$$

where Y_i ($i = 1, 2, 3$) are the aperture admittances, and Γ_i ($i = 1, 2, 3$) are the corresponding reflection coefficients using three standard loads. This equation represents a linear fractional transformation of the reflection coefficient to the admittance, based on the invariance of the cross ratio in (6).

To test this approach, we used (6) with experimental data to calculate the dielectric properties of water–dioxane

TABLE III
CALCULATED PERMITTIVITIES OF WATER-DIOXANE SOLUTIONS,
USING CORRECTION METHODS DESCRIBED IN THE TEXT

Solution	Frequency GHz	ϵ (Eq. 1)	ϵ (Eq. 2)	ϵ (Lit.)
80% water- 20% dioxane	1	64-j4	63-j4	62-j4
	3	63-j12	58-j12	60-j12
	10	45-j24	40-j26	43-j27
	18	23-j20	28-j28	27-j28
60% water- 40% dioxane	1	44-j5	44-j4	43-j5
	3	39-j10	39-j11	39-j11
	10	27-j12	22-j18	25-j18
	18	17-j9	16-j16	16-j16
40% water- 60% dioxane	1	26-j3	26-j3	26-j3
	3	22-j6	23-j7	23-j7
	10	15-j6	12-j10	14-j10
	18	10-j3	8-j7	9-j9
20% water- 80% dioxane	1	11-j1	11-j1	11-j1
	3	10-j2	10-j3	10-j3
	10	7-j1	6-j3	7-j3
	18	5+j0.5	5-j3	5-j3

The reference standards consisted of data obtained with the 2.99 mm probe immersed in water, methanol, and dioxane. The literature values were calculated using eq. (4), with the parameters given in Table II.

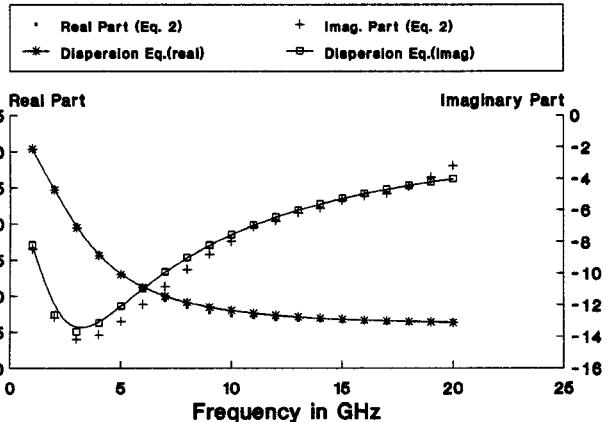


Fig. 3. Real and imaginary parts of the permittivity of methanol, measured with a 3.6 mm coaxial probe, calculated using eq. (2), compared with literature values. The calibration loads were open and short circuits and water.

mixtures. The inputs consisted of measured reflection coefficients from 2.99 mm probes in water, methanol, and dioxane ($\Gamma_1, \Gamma_2, \Gamma_3$, used for calibration) and water-dioxane mixtures. For each water-dioxane mixture, the corrected probe admittance was obtained from (6). The permittivity of the sample was then found by solving (3) iteratively using the series expansion in the Appendix. The lumped-parameter model appears to introduce substantial errors in the loss (the imaginary part of ϵ''), as shown in Table III. Marcuvitz's approximation reduces these errors.

Finally, the correction method was applied to data obtained from a probe made from 3.6 mm semirigid coaxial line, whose connector (type SMA) had a high reflection coefficient of about 0.05 at 10 GHz. The calibration loads consisted of an open and a short circuit and water; measurements were performed on 0.3 N NaCl and methanol. The results for methanol are shown in Fig. 3. The suggested calibration procedure eliminates noticeable oscillatory behavior due to connector artifacts.

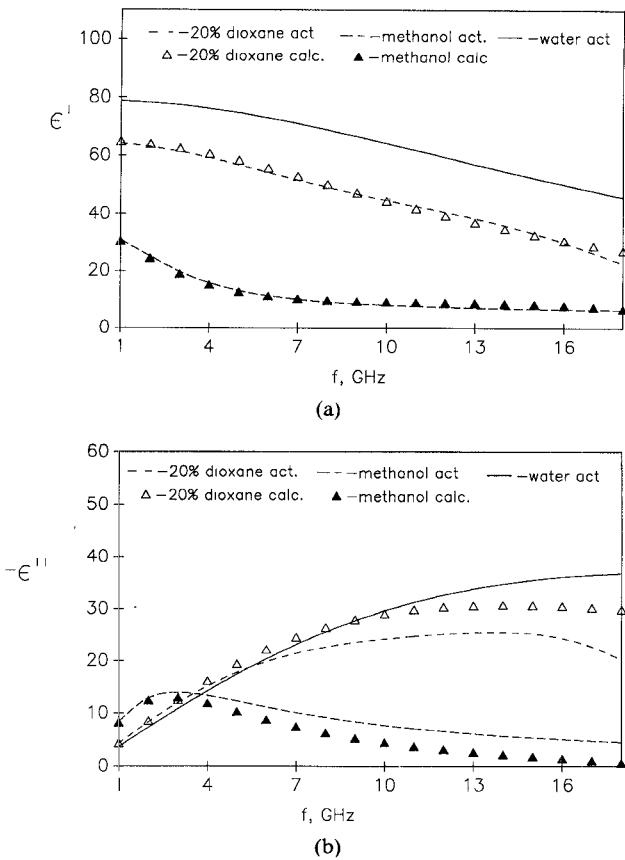


Fig. 4. (a) Real part and (b) imaginary part of the permittivity of three liquids (water, methanol, 20 percent dioxane-80 percent water), showing effects of miscalibration of ANA due to the use of lumped-parameter model (eq. (1)) for the probe. The calculations assume a 2.99 mm probe, with calibration standards consisting of open and short circuits and water.

V. USE OF LUMPED-PARAMETER MODEL IN PREVIOUS STUDIES

Several authors (notably, Stuchly and coworkers [2]–[4]) have reported extensive measurements on tissues using 3.6 mm probes at frequencies up to 10 GHz. (In most cases, the ANA was calibrated from measurements on the probe when shorted, open-circuited, and immersed in water.) Despite the use of the lumped-parameter model, they achieved high accuracy in their measurements.

To explore this further, we simulated the effects of miscalibration of the ANA that would result from using the lumped parameter model. Simulated calibration data were obtained for an open and a short circuit ($\Gamma = +1$ and -1 , respectively), and for the probe immersed in water (with Γ calculated from (3)). The assumed reflection coefficients for these measurements were $+1$ and -1 , and the probe reflection coefficient from water was calculated on the basis of (1). Then, the elements of the presumed “scattering matrix” for system errors (which actually represent errors due to the lumped-parameter model) were calculated using (5) and used to “correct” the reflection coefficients from several liquids that had been calculated using (3). Finally, the dielectric properties of the liquids were calculated using (1).

The results of this simulation are shown in Fig. 4. The permittivity values (ϵ') are remarkably accurate. In contrast, the loss (ϵ'') is underestimated above a few GHz, by about 20 percent for the water-dioxane mixture at 10 GHz, and by much larger fractions for the methanol. The previous studies [2]–[4] used a reference liquid (water) that is electrically similar to the test materials (high-water-content tissues). This is likely to ensure high accuracy in the measurements, despite errors in the model of the probe. At frequencies below ca. 1 GHz, the model-dependent errors become very small and the lumped-parameter model is satisfactory.

VI. CONCLUSION

Marcuvitz's approximation improves the accuracy of dielectric measurements using coaxial probes and is useful, for the probes considered here, up to ca. 10 GHz. The

probe technique succeeds because the errors in modeling the probe are partially canceled by calibration errors in the ANA. While the final measurement errors are difficult to quantify, they appear to be small if the electrical properties of the reference liquid are close to those of the sample under test or at low frequencies.

APPENDIX

SERIES APPROXIMATIONS TO EQUATION (3)

In the expressions below, all dimensions are in cm and all frequencies in Hz. The probe admittance Y (in siemens) is given by

$$Y = G(f) + jB(f)$$

where

$$\begin{aligned}
 B(f) &:= B1(f) + B2(f) + B3(f) + B4(f) + B5(f) + B6(f) + B7(f) \\
 \text{where} \\
 B1(f) &:= k(f) \cdot K(f) \cdot I0 & K1(f) &:= \frac{1}{Z_0 \cdot \pi \cdot \ln \left[\frac{a}{b} \right]} \cdot \sqrt{\frac{\epsilon(f)}{\epsilon c}} \\
 B2(f) &:= k(f)^3 \cdot K(f) \cdot I1 & k(f) &:= \frac{2\pi f}{c} \cdot \sqrt{\epsilon(f)} \\
 B3(f) &:= k(f)^5 \cdot K(f) \cdot I2 & \\
 B4(f) &:= k(f)^7 \cdot K(f) \cdot I3 & \\
 B5(f) &:= k(f)^9 \cdot K(f) \cdot I4 & \\
 B6(f) &:= k(f)^{11} \cdot K(f) \cdot I5 & \\
 B7(f) &:= k(f)^{13} \cdot K(f) \cdot I6 & \\
 I0 &:= 2 \cdot \int_0^\pi \sqrt{-2 \cdot a \cdot b \cdot \cos(t) + a^2 + b^2} \, dt - 4 \cdot (a + b) & \\
 I1 &:= - \int_0^\pi \frac{[-2 \cdot a \cdot b \cdot \cos(t) + a^2 + b^2]^{3/2}}{9} \, dt + 16 \cdot \frac{a^3 + b^3}{27} & \\
 I2 &:= \frac{1}{300} \cdot \int_0^\pi [-2 \cdot a \cdot b \cdot \cos(t) + a^2 + b^2]^{5/2} \, dt - \frac{64}{1125} \cdot [a^5 + b^5] & \\
 I3 &:= \frac{-1}{17640} \cdot \int_0^\pi [-2 \cdot a \cdot b \cdot \cos(t) + a^2 + b^2]^{7/2} \, dt + \frac{256}{77175} \cdot [a^7 + b^7] & \\
 I4 &:= 6.124 \cdot 10^{-7} \cdot \int_0^\pi [-2 \cdot a \cdot b \cdot \cos(t) + a^2 + b^2]^{9/2} \, dt - 1.274 \cdot 10^{-4} \cdot [a^9 + b^9] & \\
 I5 &:= -4.555 \cdot 10^{-9} \cdot \int_0^\pi [-2 \cdot a \cdot b \cdot \cos(t) + a^2 + b^2]^{11/2} \, dt + 3.446 \cdot 10^{-6} \cdot [a^{11} + b^{11}] & \\
 I6 &:= 2.471 \cdot 10^{-11} \cdot \int_0^\pi [-2 \cdot a \cdot b \cdot \cos(t) + a^2 + b^2]^{13/2} \, dt - 6.901 \cdot 10^{-8} \cdot [a^{13} + b^{13}] & \\
 G(f) &:= \sqrt{\frac{\epsilon(f)}{\epsilon c}} \cdot \left(G1(f) + G2(f) + G3(f) + G0(f) + G4(f) + G5(f) \right) &
 \end{aligned}$$

where

$$G0(f) := \frac{1}{24} \cdot [a^2 - b^2]^2 \cdot k(f)^4$$

$$G1(f) := \frac{-1}{240} \cdot [a^2 - b^2] \cdot [a^4 - b^4] \cdot k(f)^6$$

$$G2(f) := \left[\frac{1}{8960} \cdot [a^4 - b^4]^2 + \frac{1}{10080} \cdot [a^2 - b^2] \cdot [a^6 - b^6] \right] \cdot k(f)^8$$

$$G3(f) := \left[\frac{-128}{315} \cdot \left[\frac{1}{72} \cdot [a^4 - b^4] \cdot [a^6 - b^6] + \frac{1}{288} \cdot [a^2 - b^2] \cdot [a^8 - b^8] \right] \right] \cdot \frac{k(f)^{10}}{2^{10}}$$

$$G4(f) := [k(f)^{12}] \cdot \frac{36(a^2 - b^2)(a^{10} - b^{10}) + 225(a^4 - b^4)(a^8 - b^8) + 200(a^6 - b^6)^2}{2874009600}$$

$$G5(f) := [-k(f)^{14}] \cdot \frac{(a^2 - b^2)(a^{12} - b^{12}) + 9(a^4 - b^4)(a^{10} - b^{10}) + 25(a^6 - b^6)(a^8 - b^8)}{12454041600}$$

(This expansion, to fewer terms, is given in [10].) The characteristic impedance of the line is Z_0 . Note that $k(f)$ and $K(f)$ are complex functions of the complex permittivity ϵ , which is defined in the Introduction.

We have incorporated this series in the software to perform the probe measurements, using a Hewlett-Packard model HP8410 ANA controlled by a H-P 9836 computer. The permittivity ϵ can be obtained from the measured admittance within about a second. Surprisingly, the solution (using Laguerre's method [13]) showed no tendency to converge to a spurious root, perhaps because of the availability of good initial guesses for the permittivity. For measurements using the 3.6 mm probe on water at 10 GHz, all terms in this series are needed to ensure convergence of the series to (3) to within 1 percent. The rate of convergence of the series is extremely sensitive to the dimensions of the probe and to the frequency.

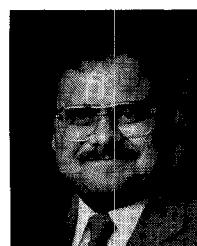
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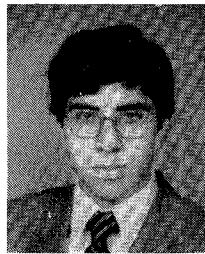
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Dr. Epstein serves as chairman of the IEEE Princeton Section of the MTT/ED/AP Societies.

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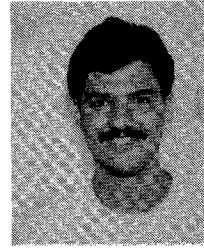
Mohinder Chabra recently graduated from the University of Wisconsin, Milwaukee with a master's degree in electrical engineering. He received a bachelor's degree in electrical engineering from the Faculty of Engineering, D.E.I., India, in July 1987.

He is now a Member of Technical Staff at AT&T Bell Laboratories, Indian Hill, Naperville, IL. His current areas of interest include software development for digital interfaces and high-frequency measurements. He intends to pursue a

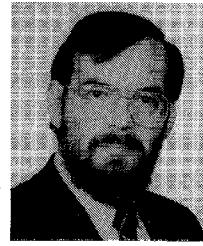
Ph.D. degree in electrical engineering.

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Mark Mirotznik (S'86) was born in Sycamore, IL, in 1965. He received the B.S. in electrical engineering from Bradley University, Peoria, IL, in 1988. He is presently a candidate for the Ph.D. degree in bioengineering from the University of Pennsylvania.



Kenneth R. Foster (M'77-SM'81-F'88) was born in Baltimore, MD, in 1945. He received the Ph.D. degree in physics from Indiana University, Bloomington, in 1971.

He served as a Lieutenant, Medical Service Corps, U.S. Navy, at the Naval Medical Research Institute, doing research on the interactions between nonionizing electromagnetic radiation and biological systems. Since 1976 he has been with the Department of Bioengineering of the University of Pennsylvania, where he is now

Associate Professor. His research interests are in the area of mechanisms of interaction between nonionizing radiation and biological systems, and dielectric properties of heterogeneous systems.

Dr. Foster is a registered professional engineer in Pennsylvania. He is a member of the AdCom of the IEEE Engineering in Medicine and Biology Society.

Benjamin R. Epstein (S'76-M'82-SM'87) received the BSE degree in electrical engineering from the University of Rochester (1979) and the MSE and Ph.D. degrees in bioengineering from the University of Pennsylvania (1980 and 1982, respectively). His Ph.D. dissertation was on the microwave dielectric properties of microemulsions. During the years 1982-83 he served as a postdoctoral fellow at the Centre National de la Recherche Scientifique, Paris, France.